

# Interpretation of non-DC components of MTs: A review

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**Definition  
and  
basic characteristics**

# Significance of moment tensor

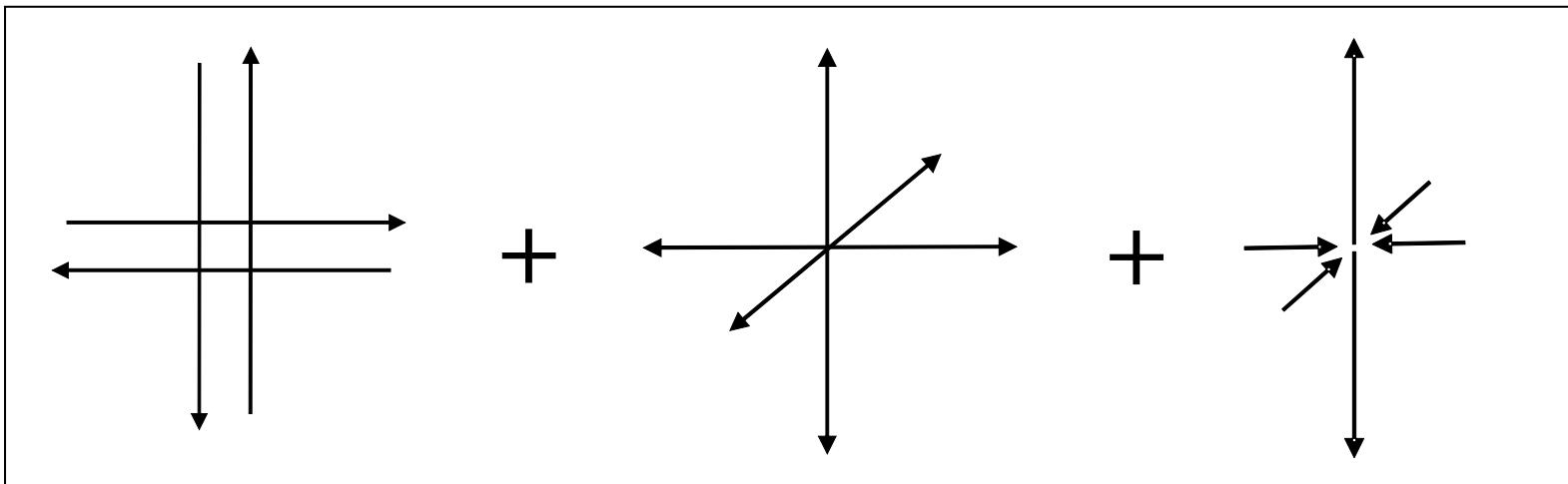
## Representation theorem

$$u_i(\mathbf{x}, t) = M_{nk} * G_{in,k}$$

↓                    ↓                    ↓  
displacement      moment      Green's  
tensor                function

## MT decomposition

$$\mathbf{M} = \mathbf{M}^{DC} + \mathbf{M}^{ISO} + \mathbf{M}^{CLVD}$$



DC  
shear

ISO  
non-shear

CLVD  
non-shear

# Moment tensor in isotropic media

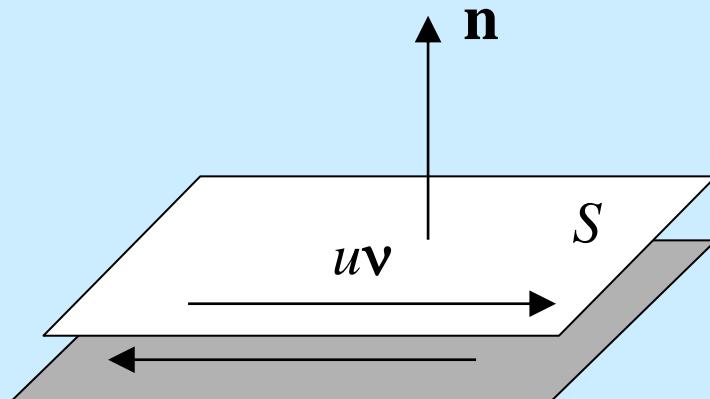
## Shear earthquakes in isotropy

(Aki & Richards 2002, Eq. 3.22):

$$M_{kl} = \mu u S (\nu_k n_l + \nu_l n_k)$$

$$M_{kl} = M_0 \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

double-couple (DC)



$u$  – slip

$S$  – fault area

$\mu$  – shear modulus

$\mathbf{v}$  – slip direction

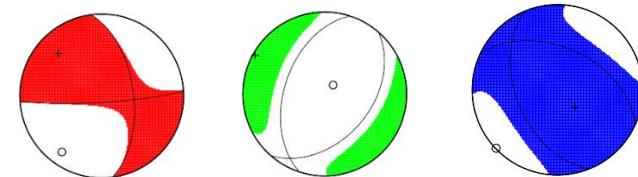
$\mathbf{n}$  – fault normal

$c_{ijkl}$  – elastic parameters

# Basic characteristics of non-DC components

## Indications of non-DC:

- P-wave radiation pattern
- anomalous P/S amplitude ratio



## Areas with non-DC seismicity:

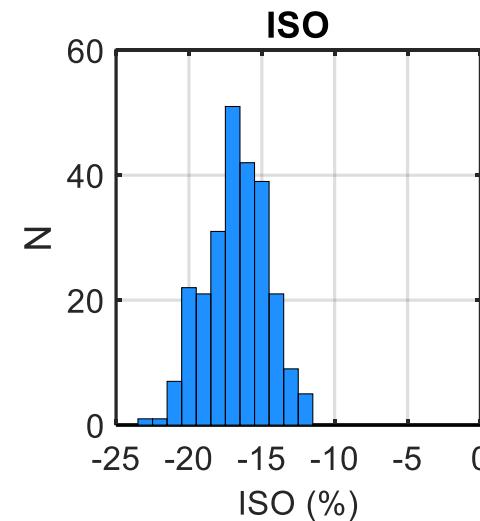
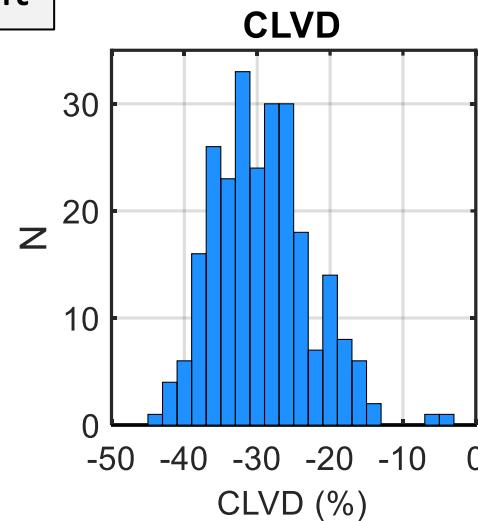
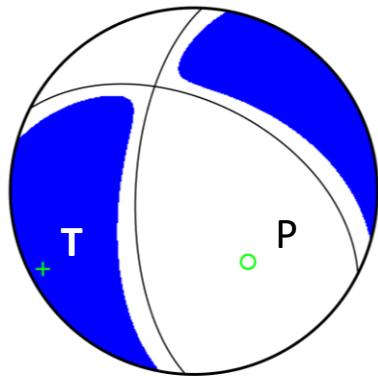
- geothermal and volcanic regions,
- complex fractured zone with interacting fault segments
- steep slopes with landslides
- subducting slabs
- mines, oil and gas fields

## Physical processes

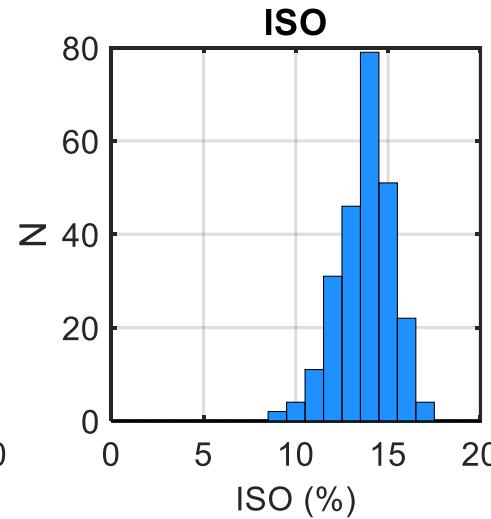
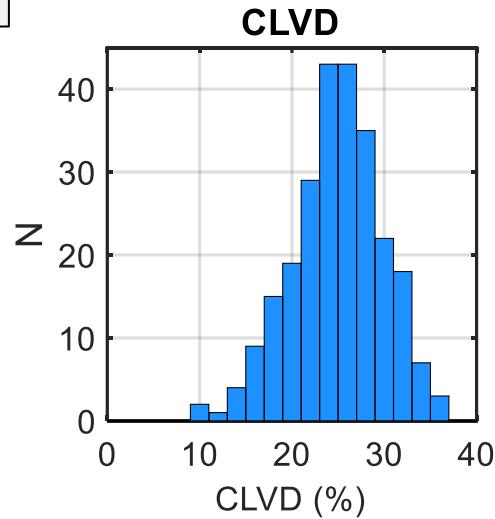
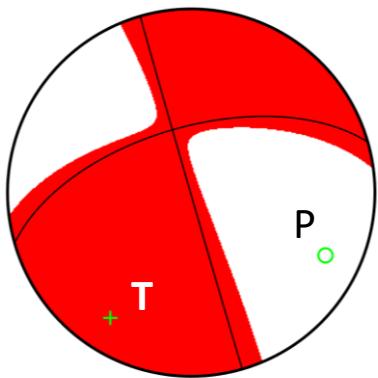
- magma and fluid flow in rocks
- stress anomalies related to complex fault geometry
- tensile stress regime
- shear faulting in anisotropic focal zone
- anthropogenic activities (hydrofracking, fluid injection, fluid extraction, mining, chemical and nuclear explosions)

# Example 1: non-DC earthquakes in West Bohemia

Compressional event



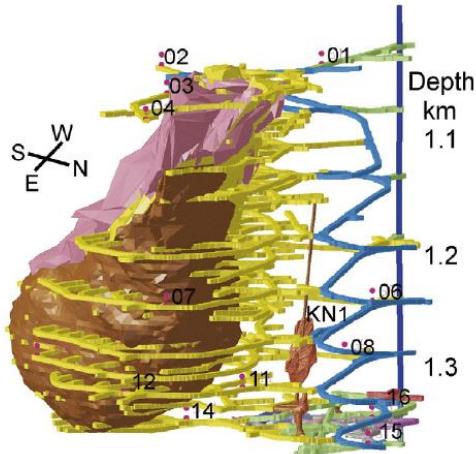
Extensional event



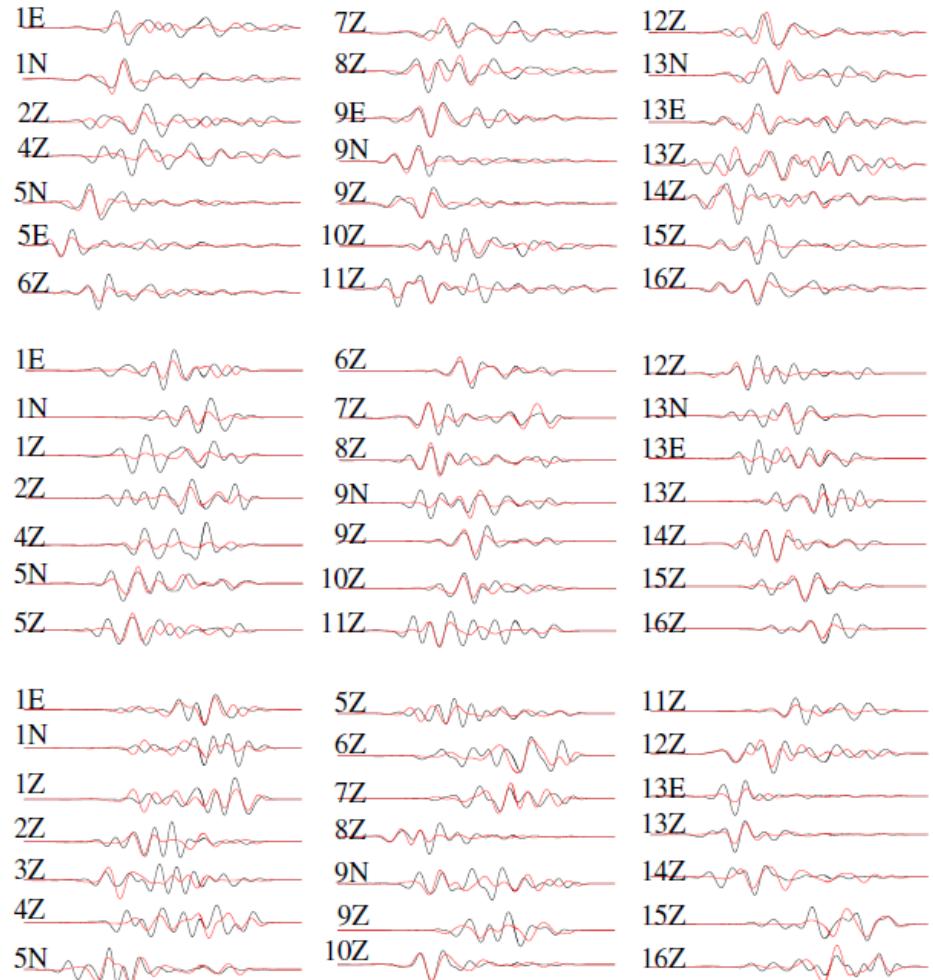
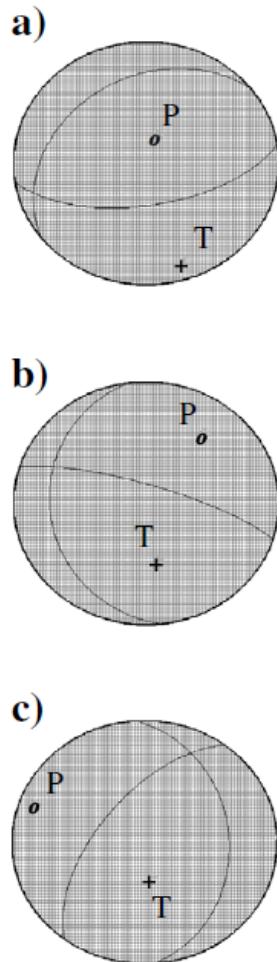
## Example 2: Non-DC events in mines

### Pyhasalmi ore mine, Finland

- depth of 1.4 km
- ore forms a potato-shaped body
- 16 geophones (4.5 Hz)
- sampling rate - 3000 Hz



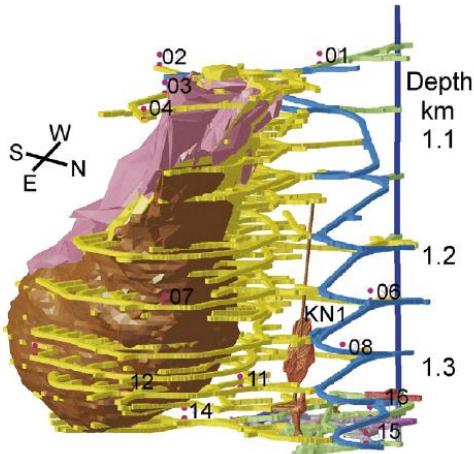
### Explosions in mines



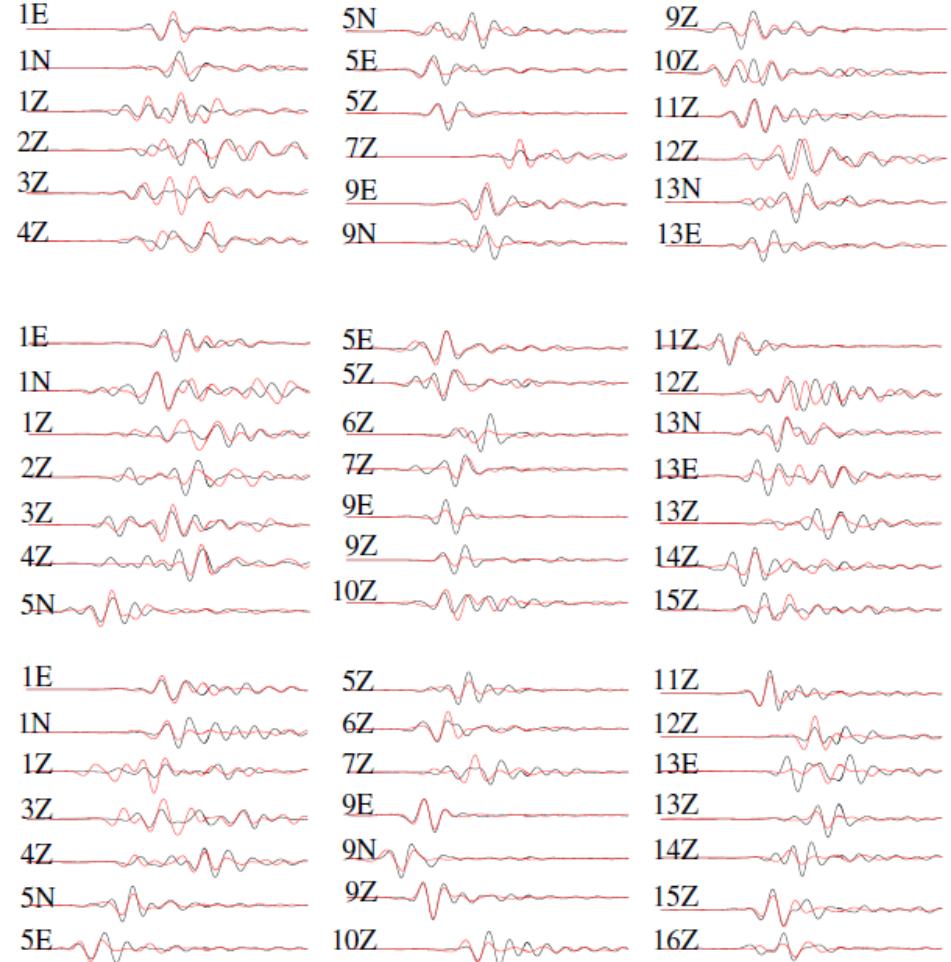
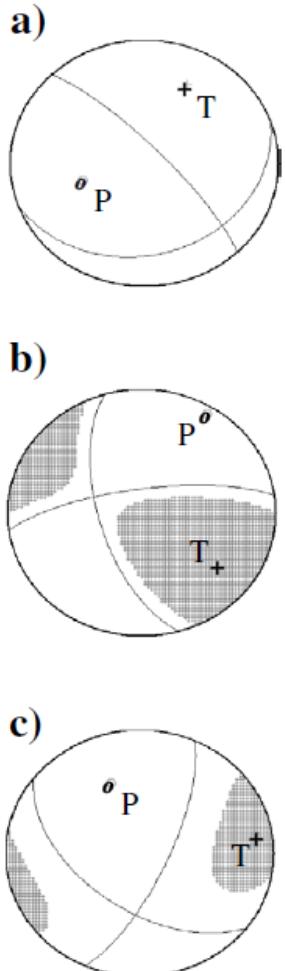
# Example 3: Non-DC events in mines

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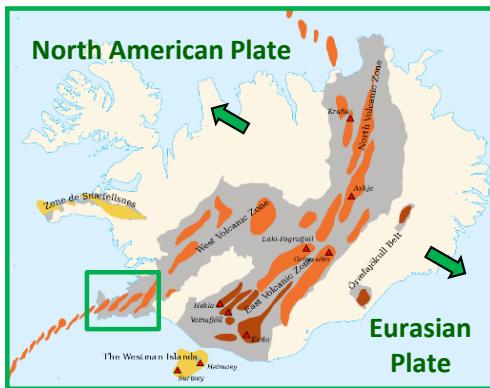


## Rockbursts in mines



# Example 4: Non-DC events in Iceland volcanic region

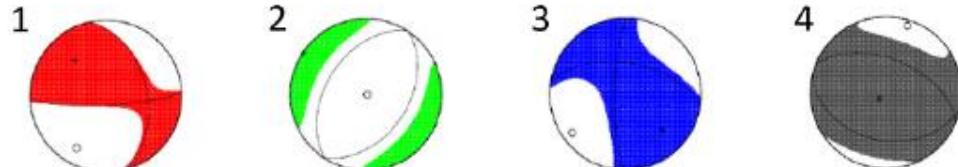
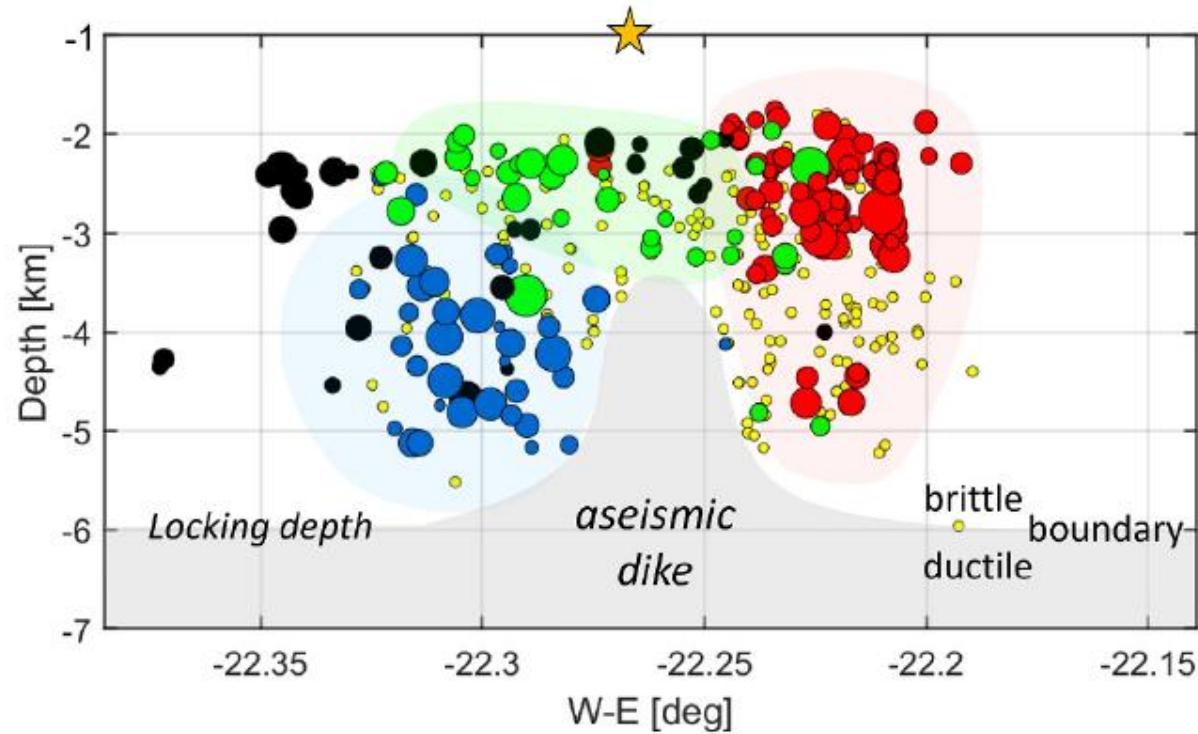
Seismicity in Reykjanes Peninsula before the 2021 Fagradalsfjall volcano eruption



Mid-Atlantic Ridge –  
slow-spreading rift

## REYKJANET network

16 BB local seismic  
stations  
sampling rate 250 Hz  
epicentral distance:  
up to 20-25 km



**Non-DC components:  
irregular fault geometry**

# Complex shear faulting: schemes

## Multiple (non-interacting) events

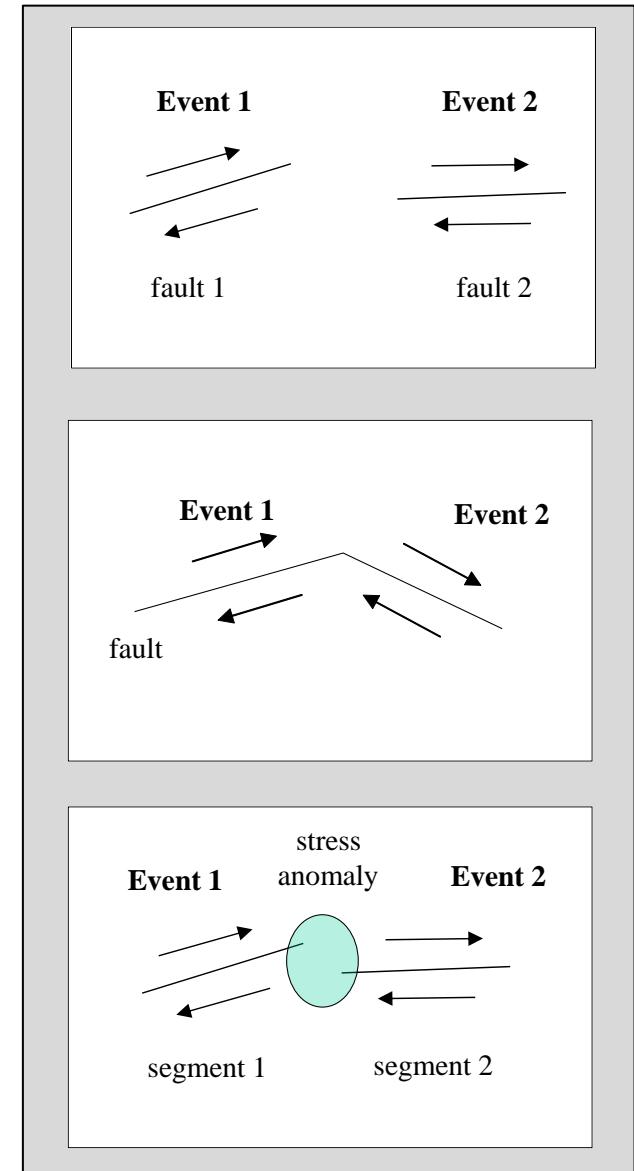
- subsequent independent events
- simultaneous occurrence in time
- different faults

## Irregular fault geometry

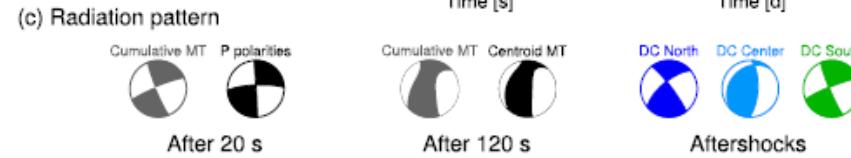
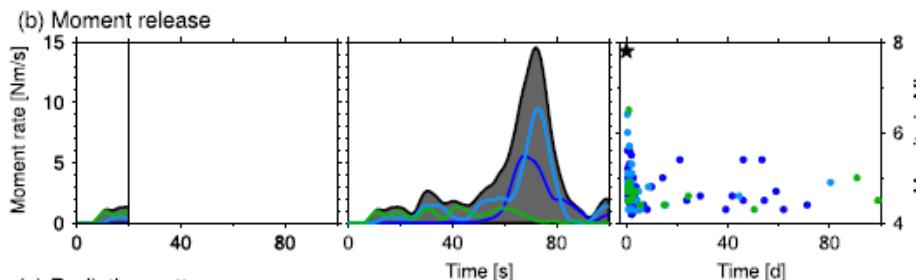
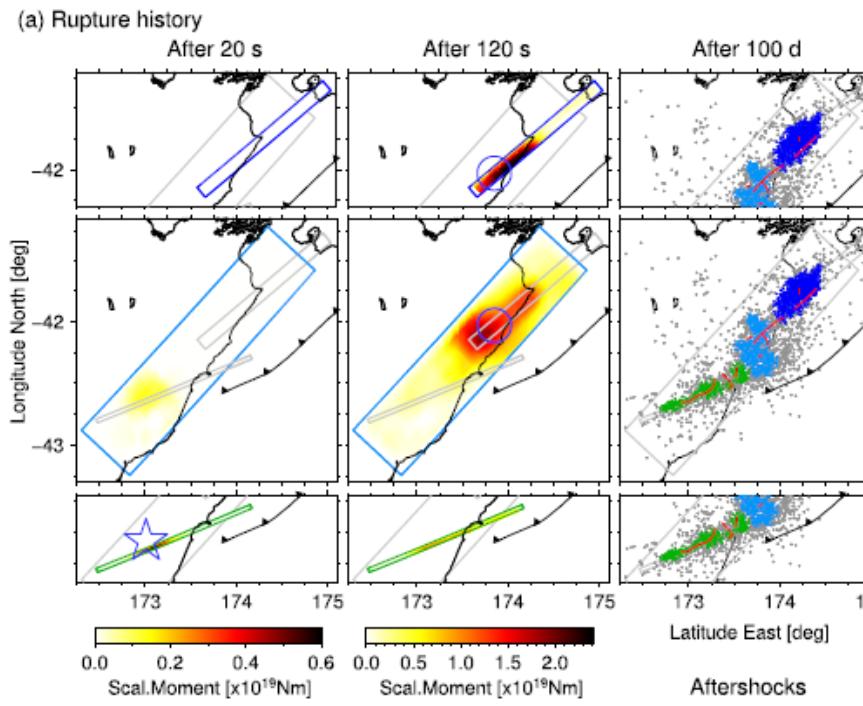
- smooth bending of faults
- sharp bending of faults
- differently oriented segments

## Fault segment interaction

- isolated interacting segments
- fault steps
- local stress anomaly due to interaction



# Complex shear faulting: fault steps



Cumulative MT   Centroid MT



After 120 s

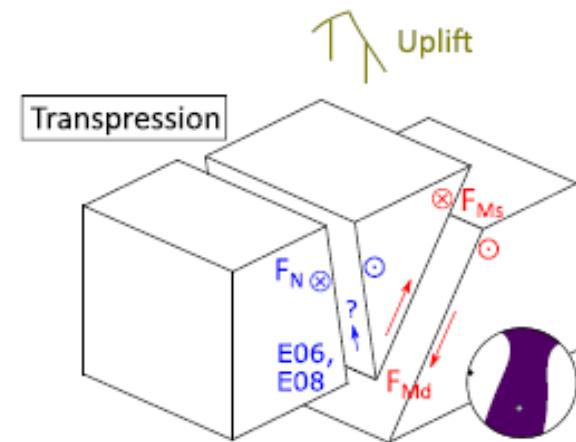
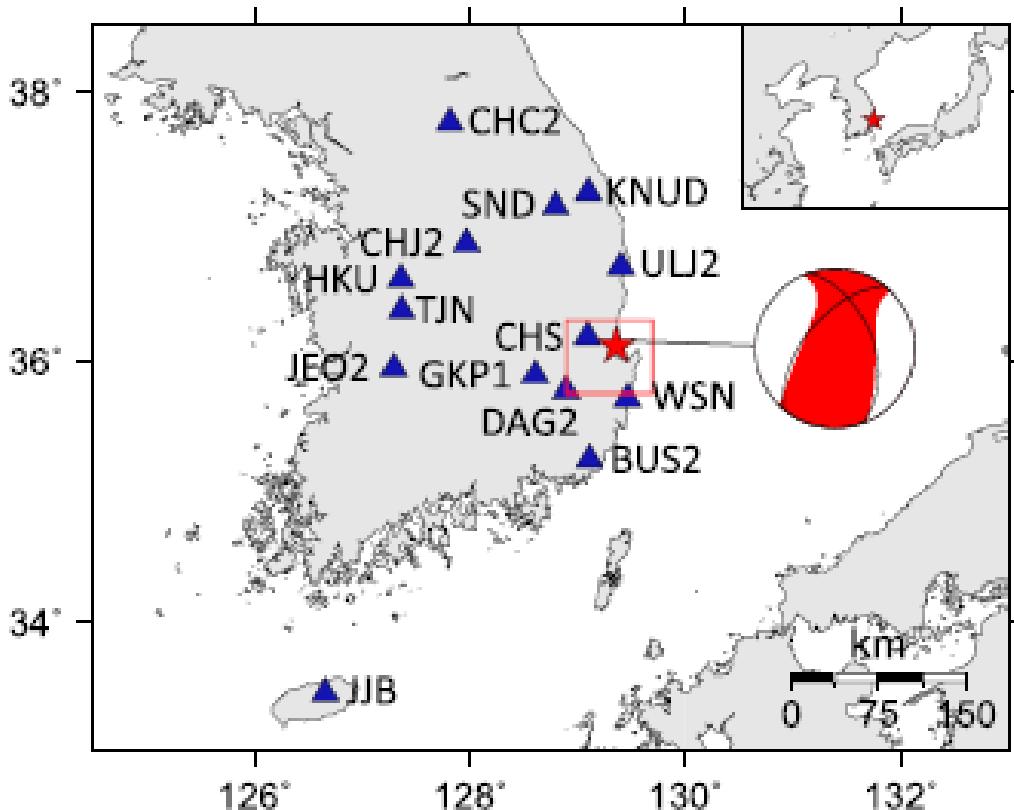
**Mw 7.8 2016  
Kaikoura earthquake,  
New Zealand**

- depth of 15 km
- surface deformations
- uplift up to 8 m
- interaction of two faults

# Complex shear faulting: activation of several fault segments

## 2017 Pohang earthquake (Mw 5.4)

- triggered by fluid injections in a geothermal reservoir

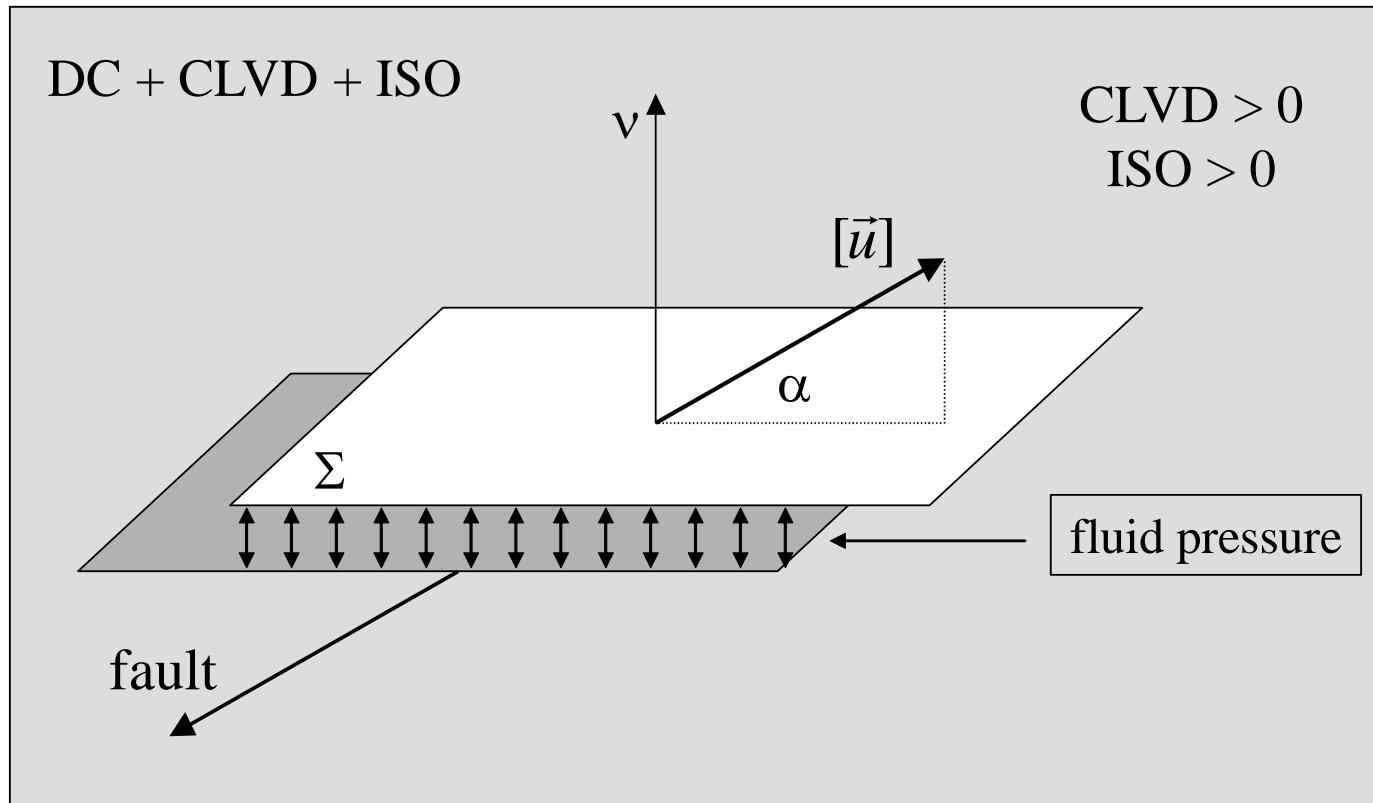


- oblique contraction
- joint movement of two intersecting faults
- reverse and strike slip movements

**Non-DC components:  
tensile/compressive faulting**

## Tensile faulting: scheme

### Opening or closing of a fault during shear rupture

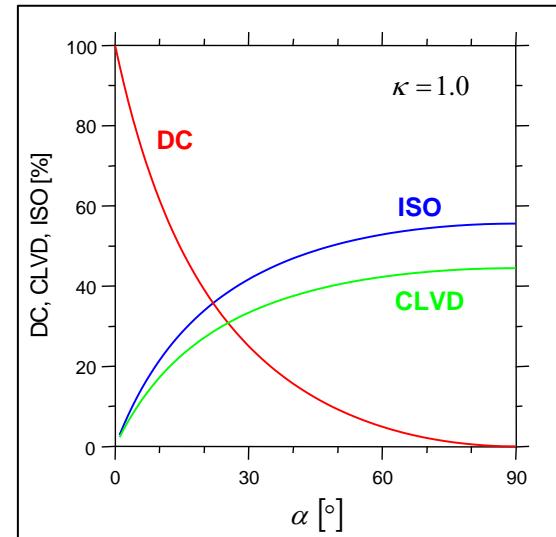
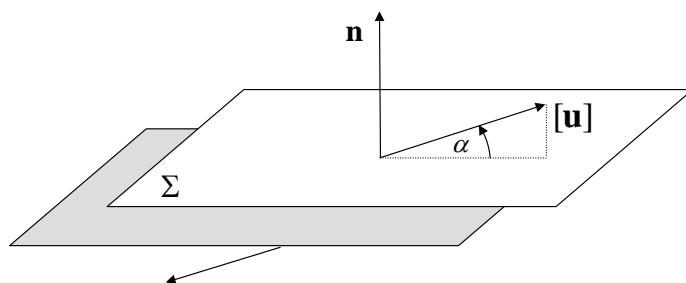
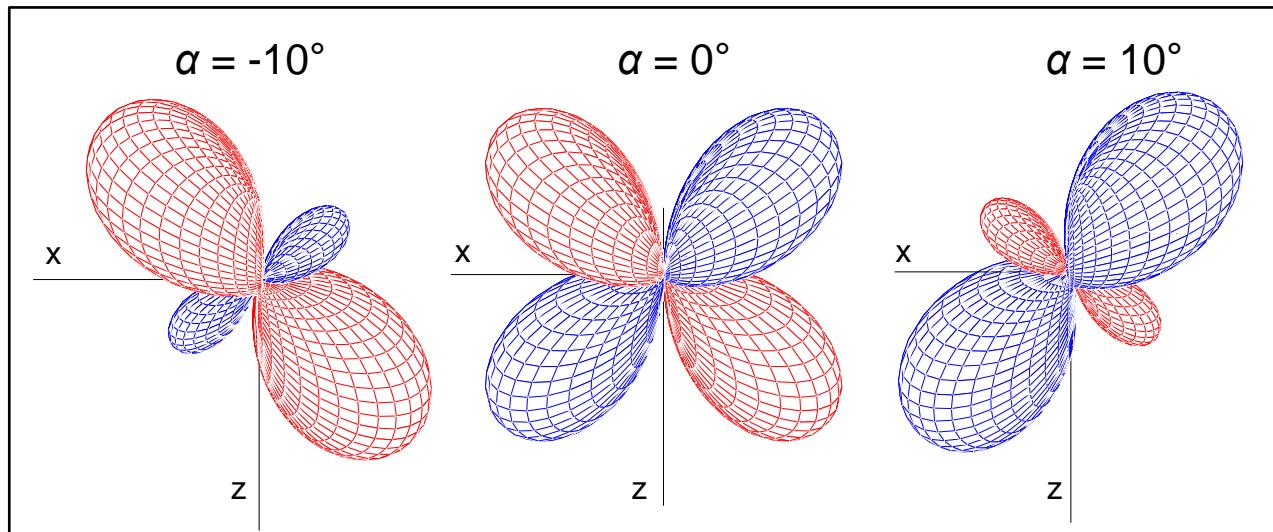


**Example:** hydrofracturing

- high pore pressure can cause opening faults during the rupture process
- CLVD and ISO are positive

# Shear-tensile faulting: radiation pattern

Radiation pattern as a function of the slip deviation  $\alpha$

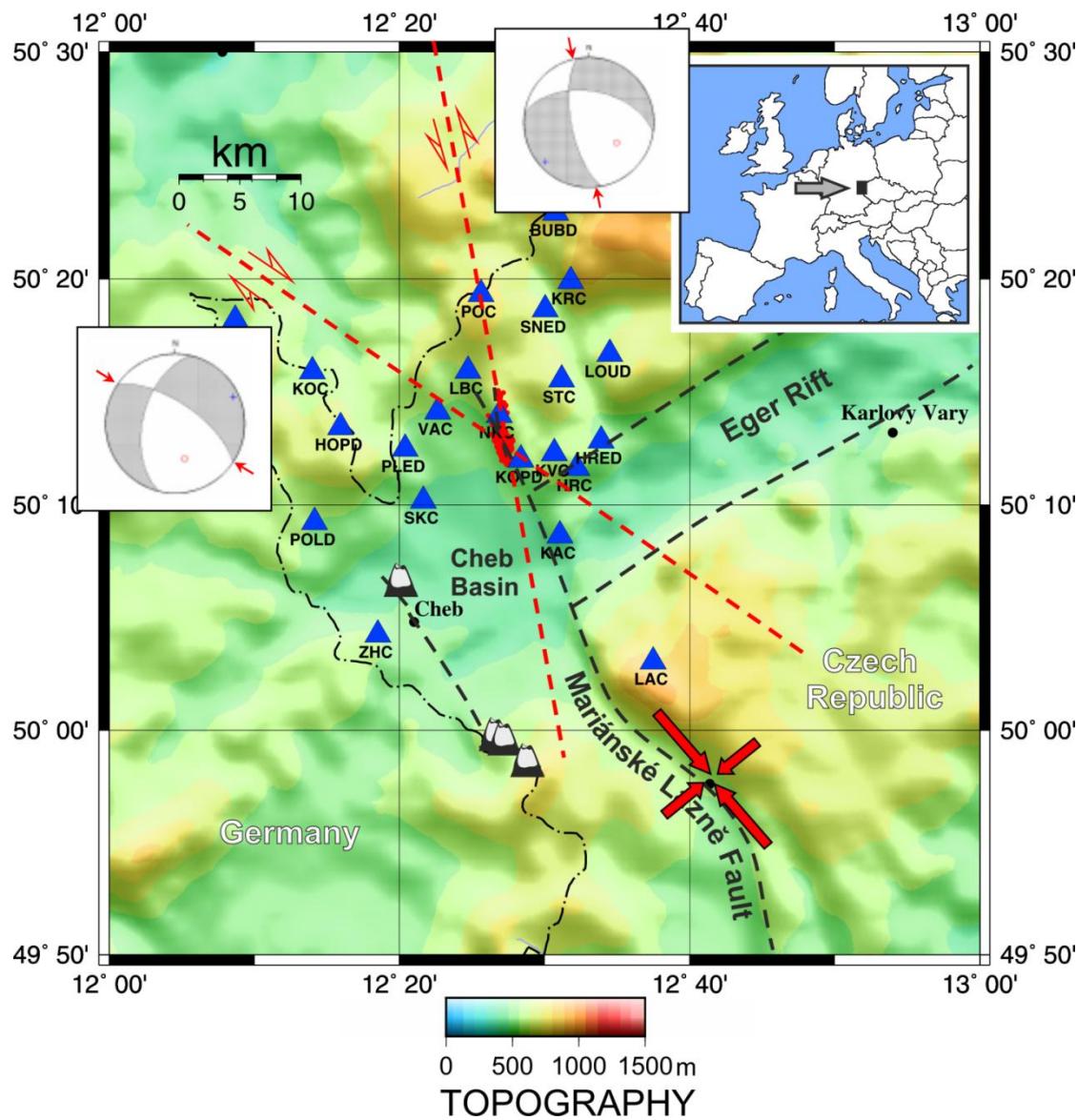


$\alpha = 10^\circ$



DC = 60 %  
non-DC = 40 %

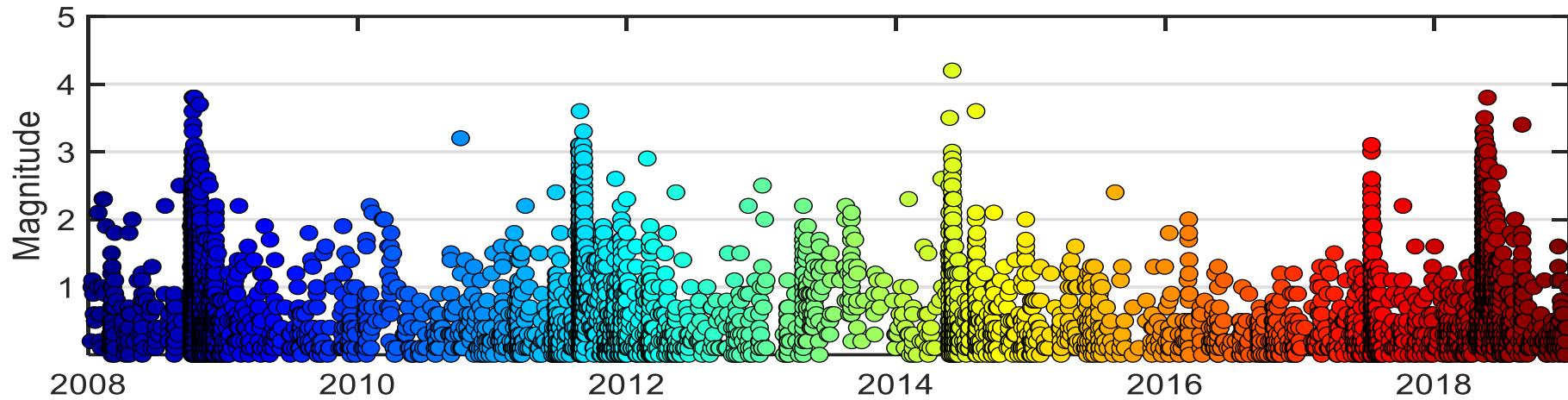
# Swarm area in West Bohemia, Czech Republic



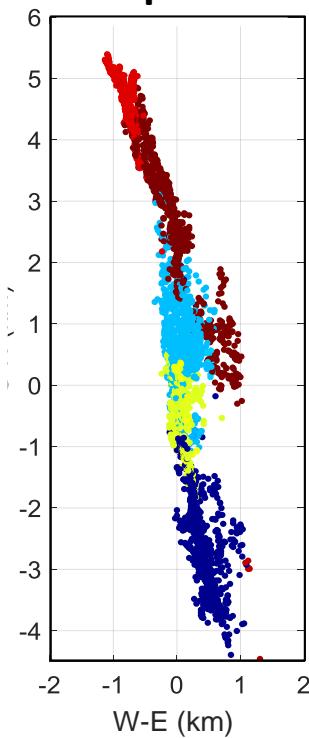
## Geodynamically active area:

- Intersection of two major fault systems
- Persistent seismicity
- Emanations of CO<sub>2</sub> rich fluids
- Springs of mineral water
- Quaternary volcanoes

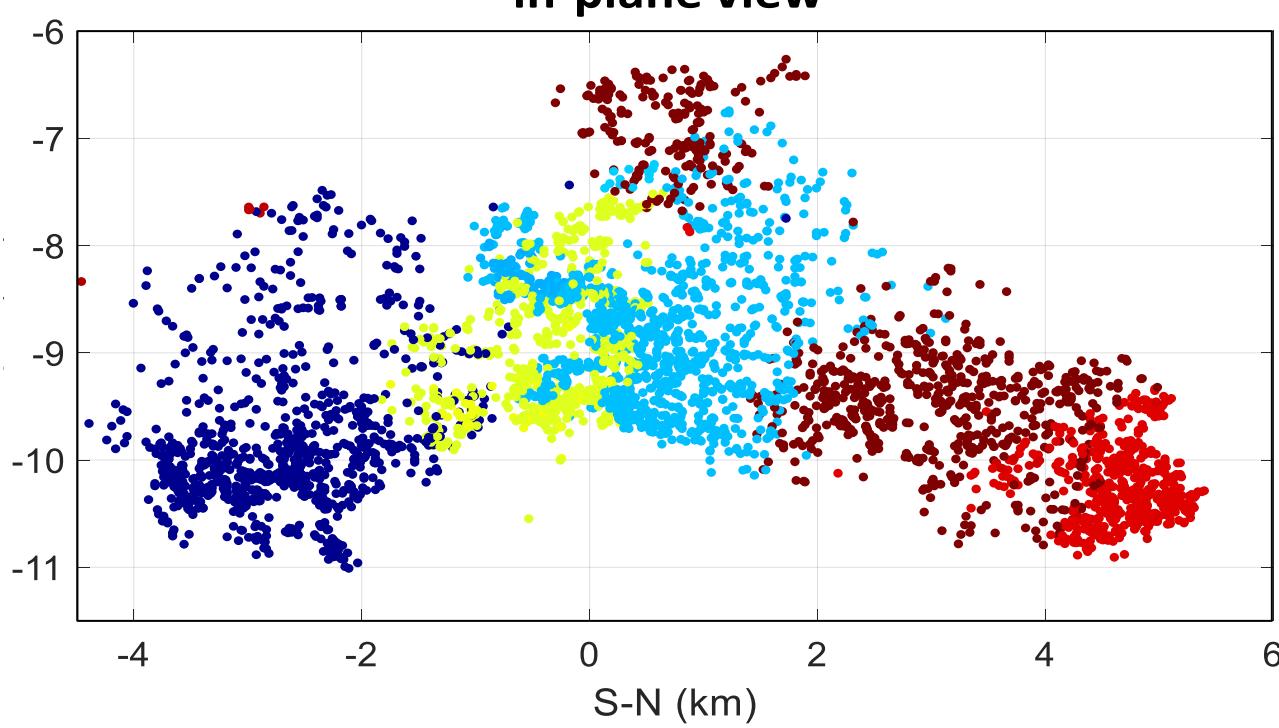
# West Bohemia earthquake locations: period 2008-2018



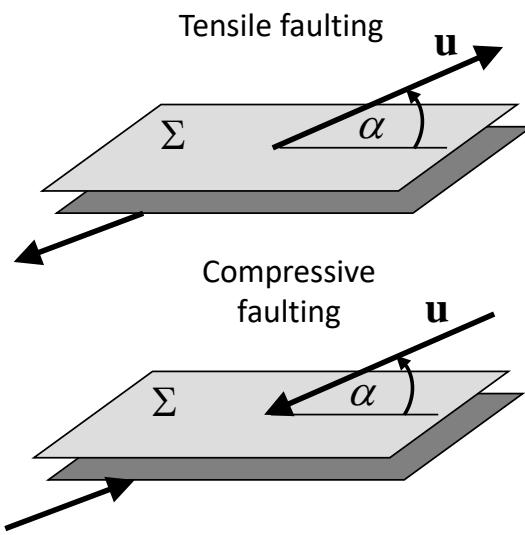
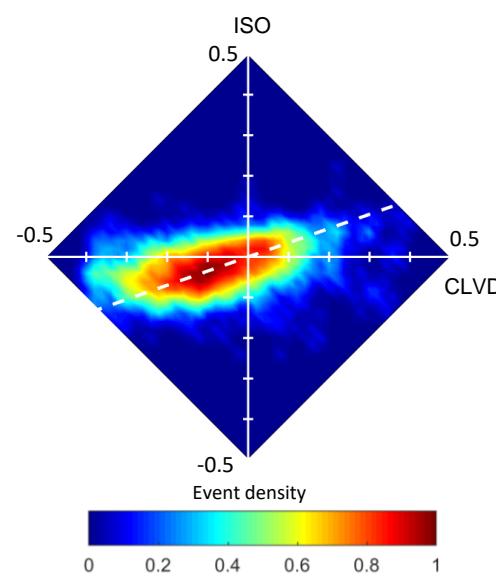
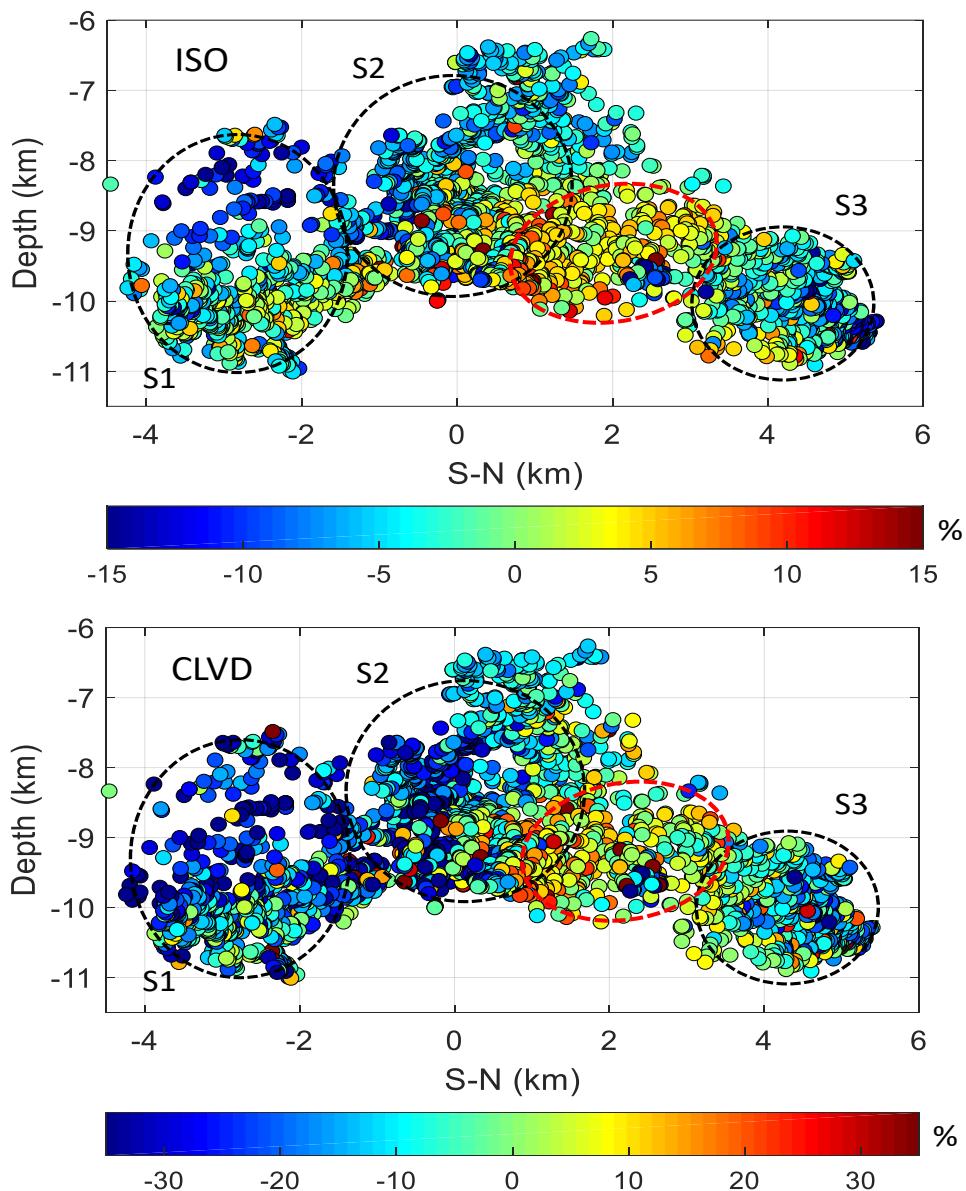
map view



in-plane view



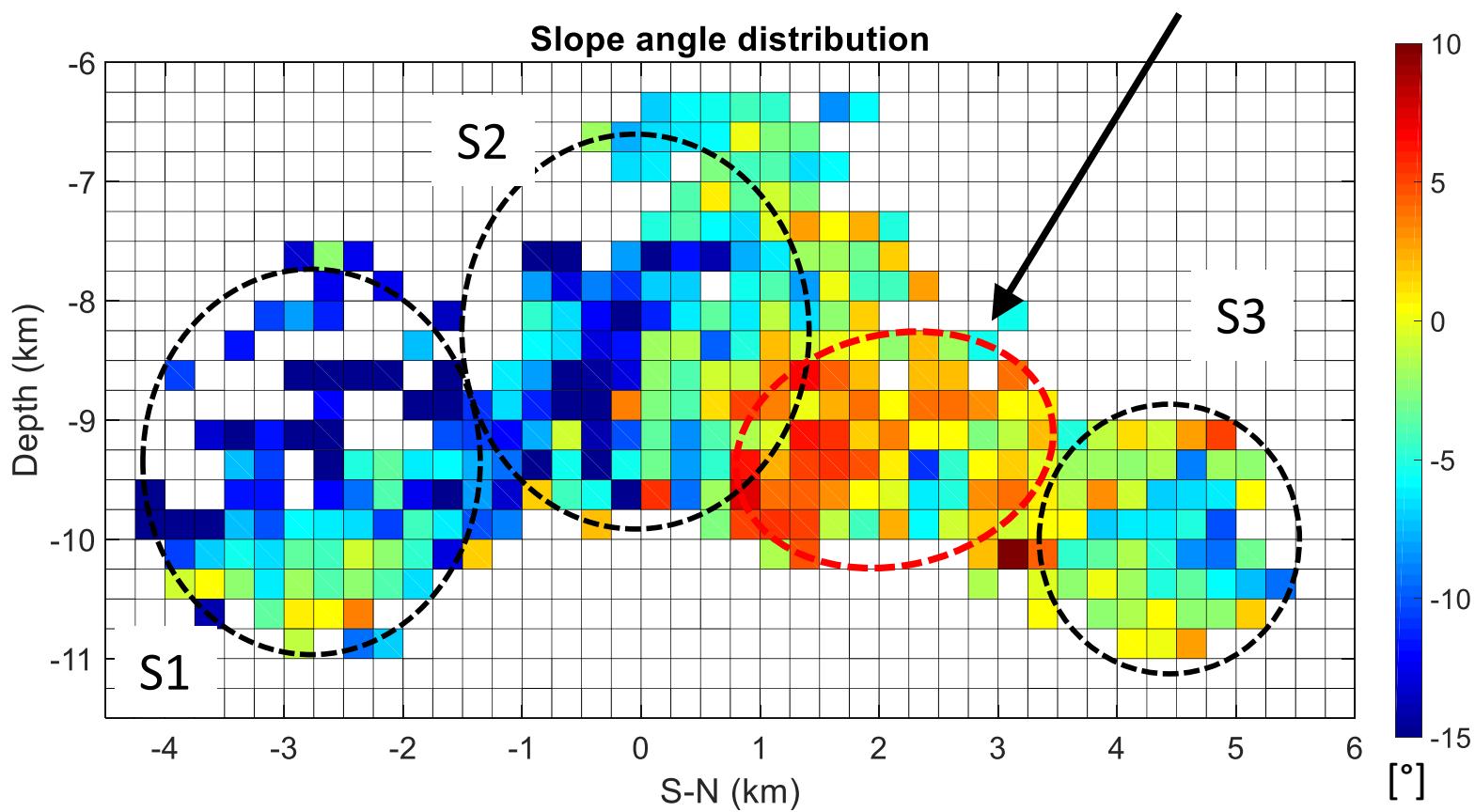
# Non-DC components for shear-tensile faulting



# Opening/closing of a fault: West Bohemia

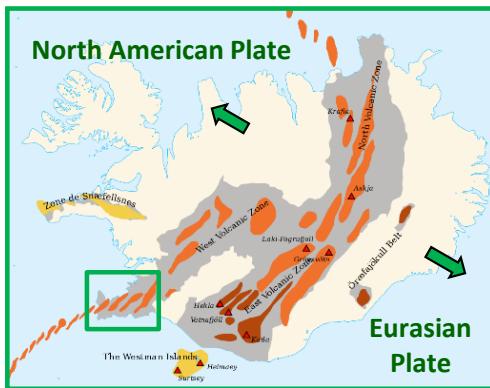
## Mapping of fluid flow

tensile stress  
anomaly

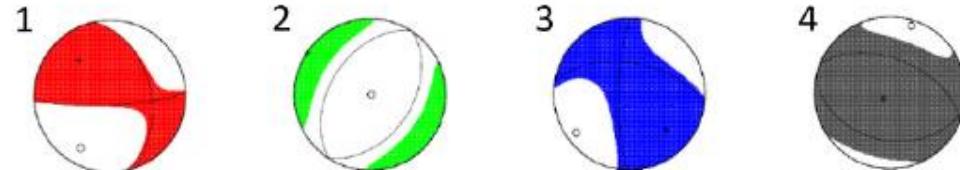
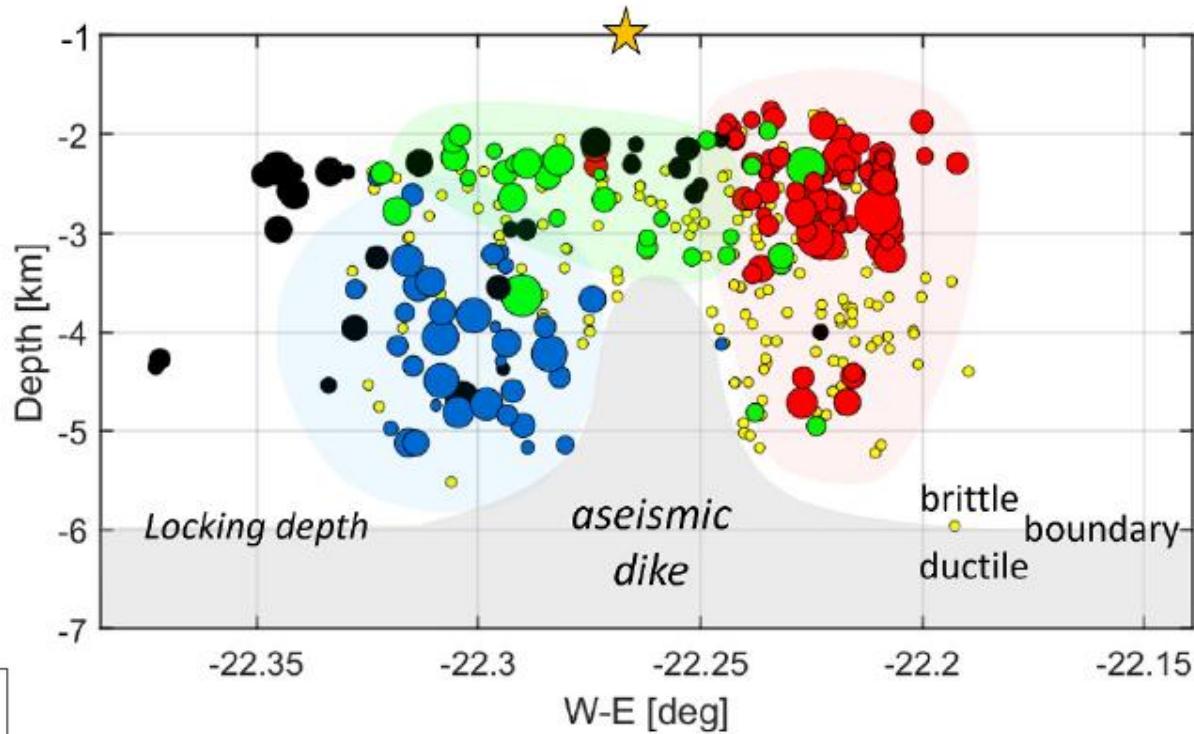
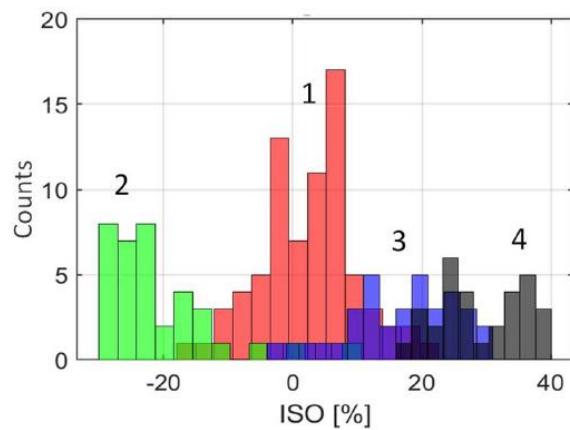


# Tensile/compressive faulting in Iceland volcanic region

Seismicity in Reykjanes Peninsula before the 2021 Fagradalsfjall volcano eruption



Mid-Atlantic Ridge –  
slow-spreading rift



Hrubcová & Vavryčuk (EPSL, 2022; Tectonophysics, 2023)

**Non-DC components:  
seismic anisotropy**

# Shear faulting in anisotropic media

## Shear earthquakes in anisotropy

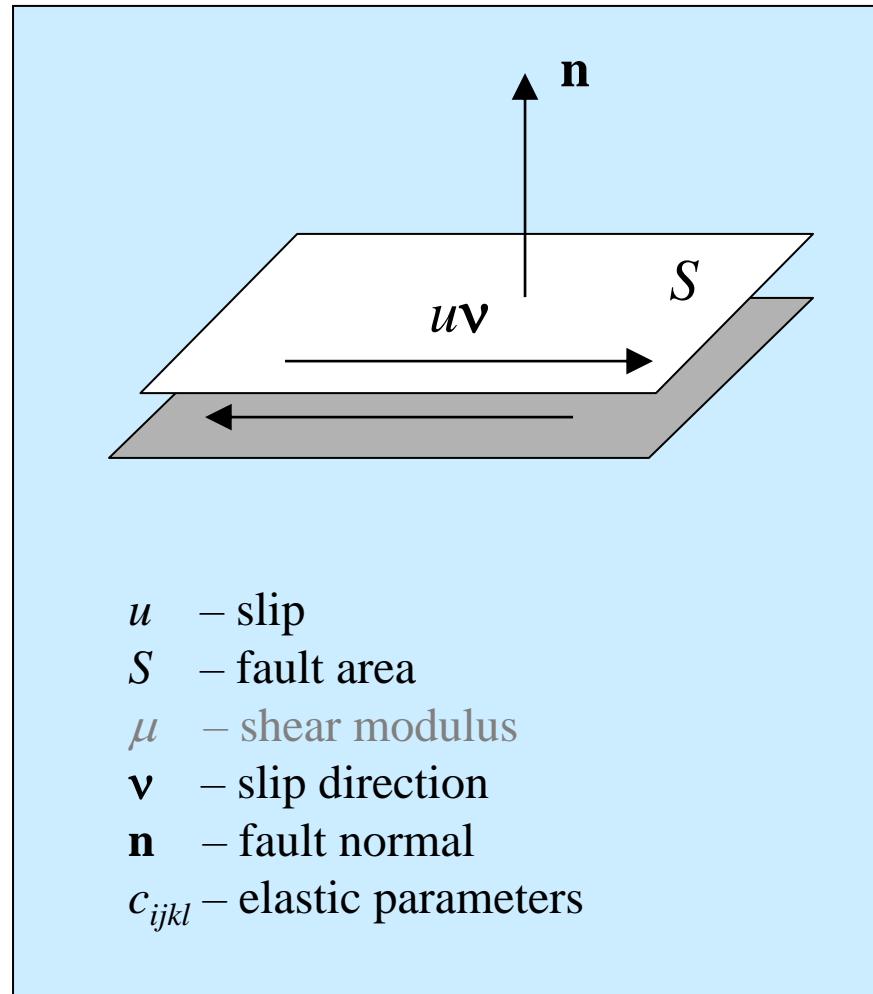
(Aki & Richards 2002, Eq. 3.19):

$$M_{kl} = u S c_{ijkl} \nu_k n_l$$

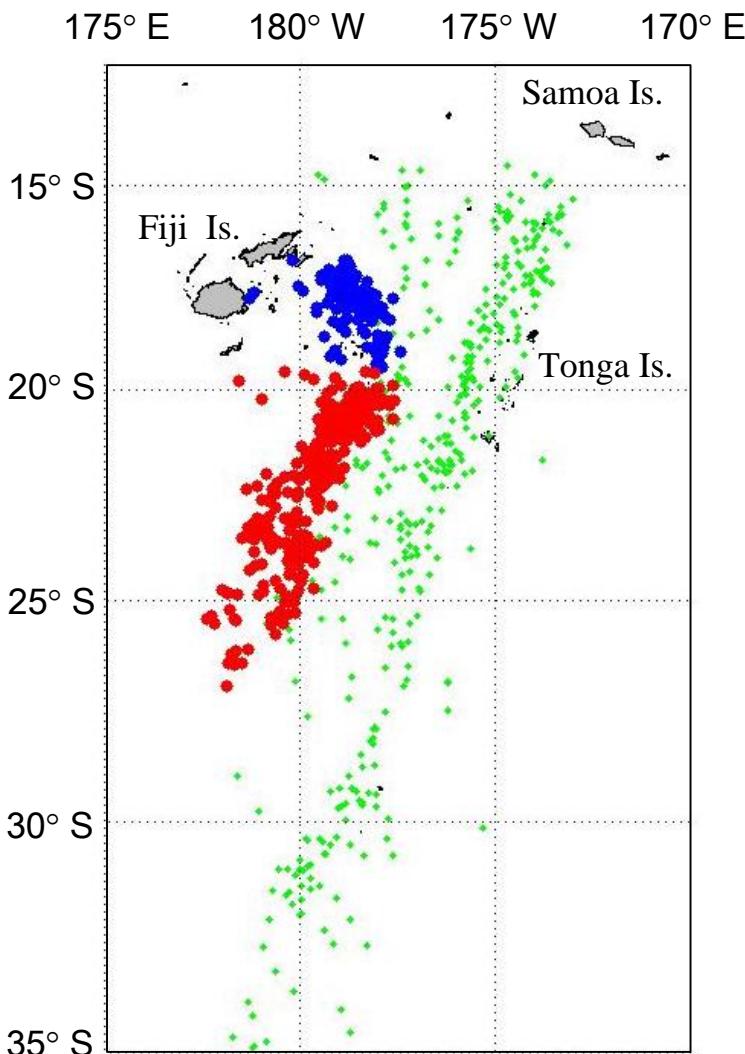
$$M_{kl} = \begin{bmatrix} M_{11} & M_{12} & M_{13} \\ M_{12} & M_{22} & M_{23} \\ M_{13} & M_{23} & M_{33} \end{bmatrix}$$

full (non-DC) moment tensor

DC + CLVD + ISO



# Deep earthquakes in the Tonga subduction slab



Harvard MT solutions  
(M>5, 1980-2002)

## Tonga subduction

Pacific Plate subducts under the Australian Plate

Plate velocity is 10.5 cm/yr

Azimuth of the Tonga Trench is N210°E

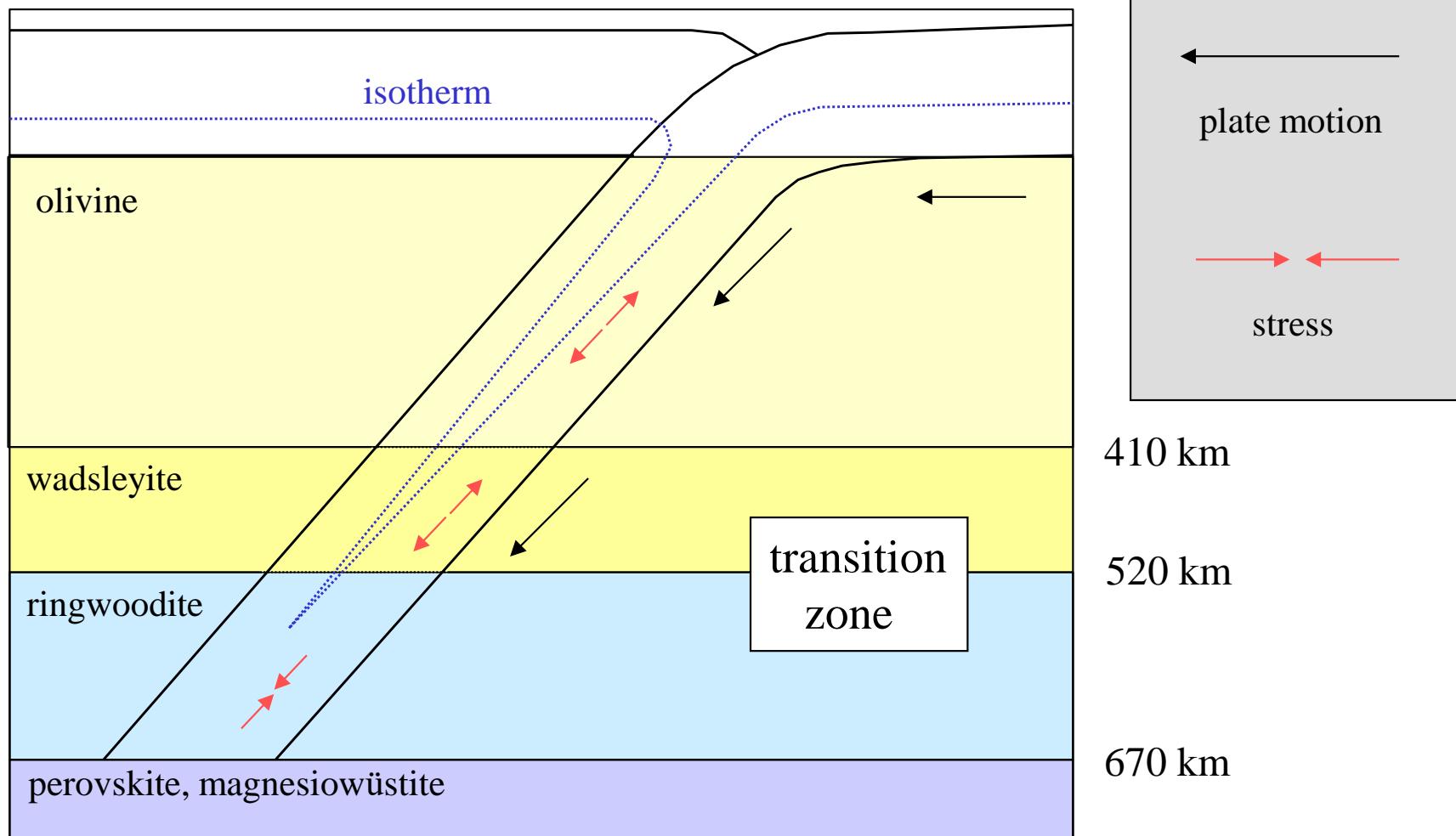
Dip of the subducting slab is 60°

The highest deep seismicity in the world

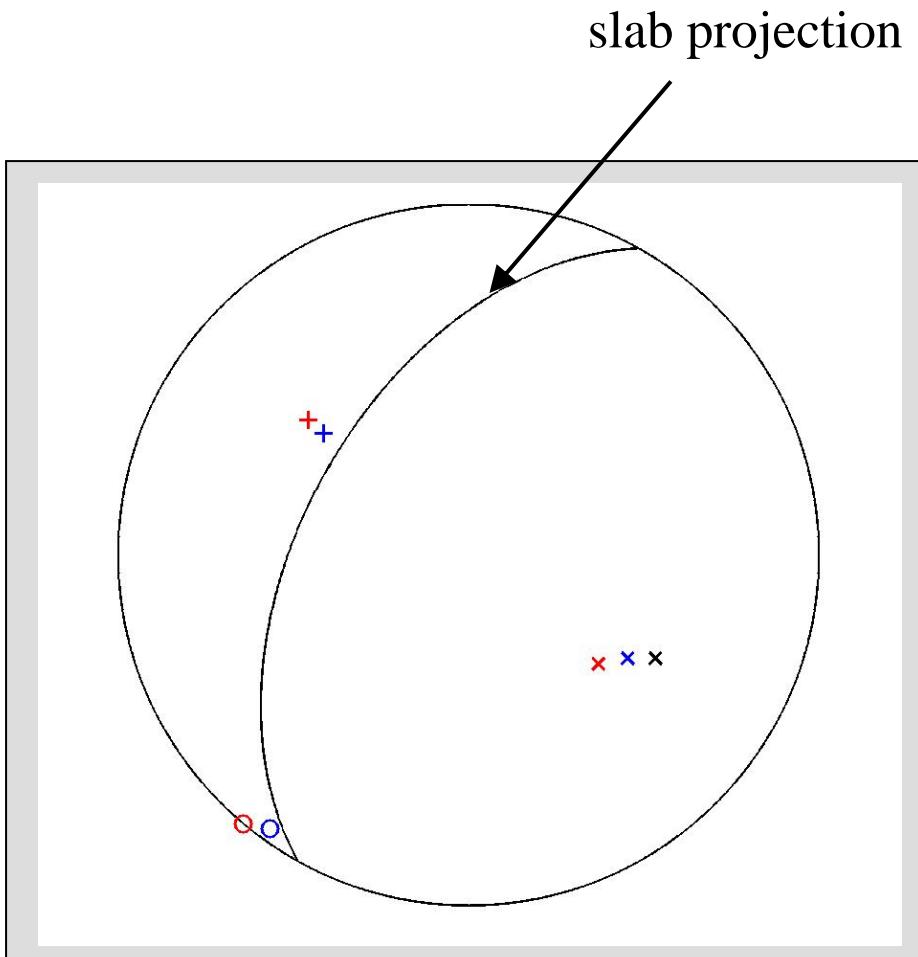
- depth 100-500 km
- **depth 500-700 km, southern cluster** ←
- depth 500-700 km, northern cluster

Vavryčuk (JGR, 2004; PEPI, 2008)

# Slab geometry and mantle composition



# Orientation of slab, stress and anisotropy



- x - normal of slab
- x - stress
- x - anisotropy

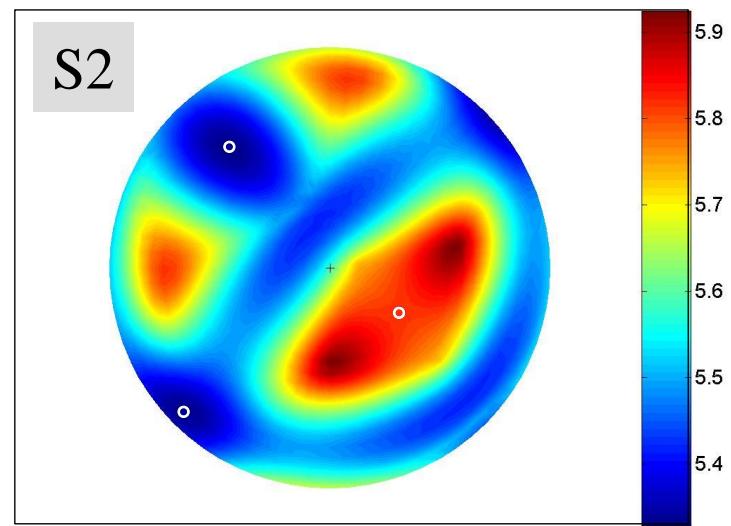
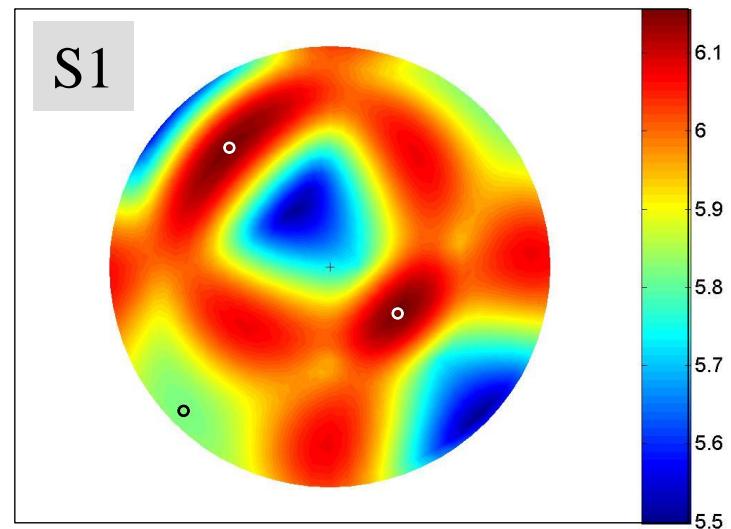
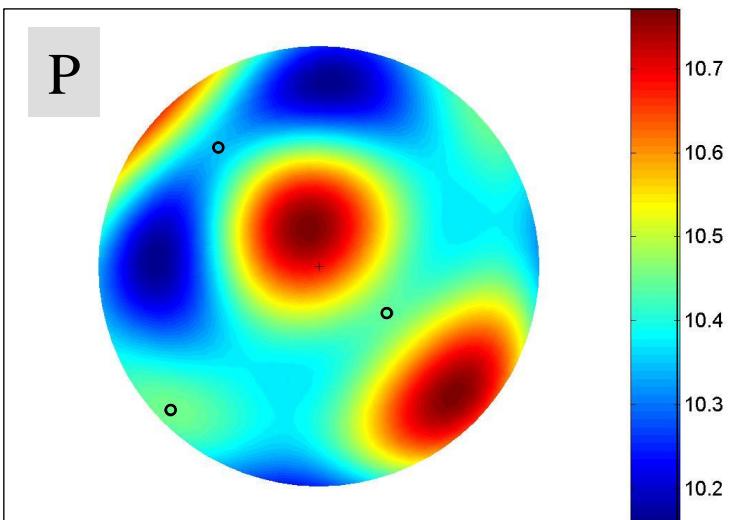
Maximum compression is along the slab (“down-dip compression”)

Stress and anisotropy orientations coincide

Anisotropy is stress induced!

Vavryčuk (JGR, 2004; PEPI, 2008)

## Predicted velocities in the slab

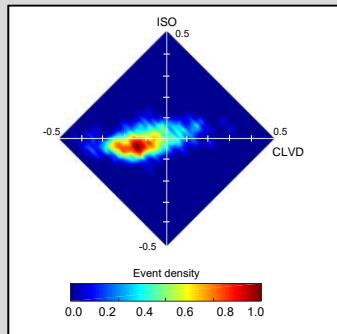


**P-wave anisotropy: 6%,**  
**S1-wave anisotropy: 11%**  
**S2-wave anisotropy: 10%**

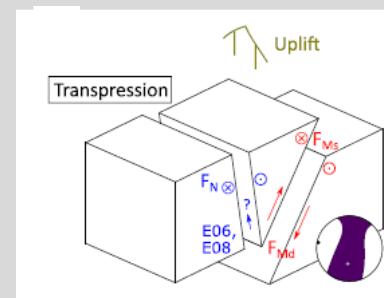
# Summary

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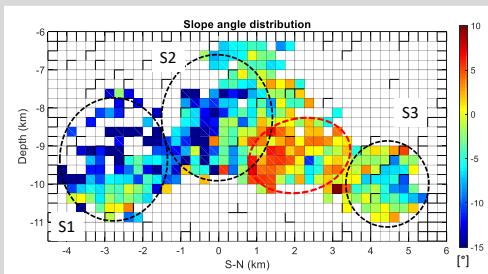
Non-DC components provide essential information about faulting, tectonic stress and physical properties of material in the focal zone



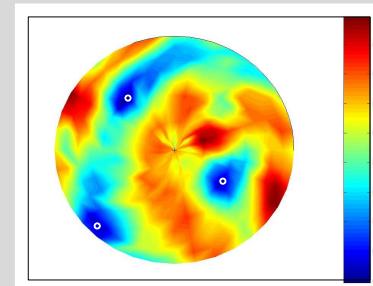
Shear-tensile  
faulting



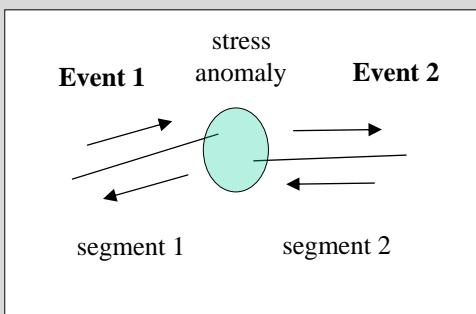
Understanding  
complexities of  
fracturing



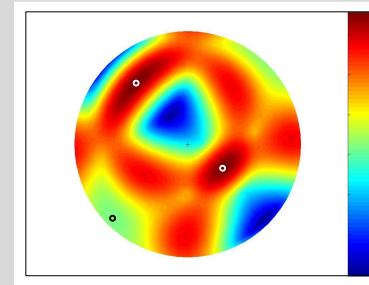
Mapping of fluid  
flow and rock  
compaction



Orientation  
of anisotropy  
in focal area



Detection of  
stress anomalies  
and fault  
interactions



Velocities of  
P, S1 and S2  
waves in  
focal area